Predator-prey and competitive models with seasonality: an overview of recent results

<u>Carlota Rebelo</u>¹, Isabel Coelho², Maurizio Garrione³, Cinzia Soresina⁴ and Elisa Sovrano⁵

¹CEMAT and Departamento de Matemática, Faculdade de Ciências, Universidade de Lisboa, Portugal

² CEMAT, Instituto Superior de Engenharia de Lisboa, Portugal ³Department of Mathematics, Politecnico di Milano, Italy

⁴ Institute of Mathematics and Scientific Computing, University of Graz, Austria

⁵ Universià degli Studi di Modena e Reggio Emilia, Italy

 $Corresponding/Presenting\ author:\ mcgoncalves@fc.ul.pt$

Talk Abstract

In this talk we will consider predator-prey and competition models. We will give an overview of recent results in the case when seasonality is considered.

In what concerns predator-prey models we prove persistence results and also coexistence ones both with a logistic type growth for the prey or, in the case of two species, considering an Allee effect (both the cases of weak and strong Allee effects). These results were obtained for a general class of functional responses.

In the case of competition models, we analyse in detail the case of a twospecies competition model in which competition can be quite general. We give conditions for the extinction of one or both species and for coexistence.

The results obtained with topological methods are described in the papers [1, 2, 3].

Keywords: predator prey, competition, persistence, extinction, coexistence.

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References

- [1] Coelho, I., Rebelo, C., Sovrano, E., Extinction or coexistence in periodic Kolmogorov systems of competitive type, *Discrete Contin. Dyn. Syst.*, 41, 2021, pp. 5743-5764.
- [2] Garrione, M., Rebelo, C., Persistence in seasonally varying predator-prey systems via the basic reproduction number, *Nonlinear Anal. Real World Appl.*, 30, 2016, pp. 73-98.
- [3] Rebelo, C., Soresina, C., Coexistence in seasonally varying predator-prey systems with Allee effect, *Nonlinear Anal. Real World Appl.*, 55, 2020, 103140, 21 pp.